

Appendix

Chapter 2:

$$A_4 = \frac{(1+R)(1+0.5R)}{RbM^2}$$

$$A_7 = \frac{-1}{M^2}$$

$$a_2 = \frac{2M^2Rb}{(1+R)(1+0.5R)}$$

$$A = \frac{a_3}{a_2}$$

$$q_1 = \sqrt{\frac{a_1}{2}}$$

$$v_1 = \sqrt{\frac{\sqrt{\frac{a_1^2}{4} + \frac{p^2}{4}} + \frac{a_1}{2}}{2}}$$

$$b_2 = p_2^3 A_4$$

$$b_5 = b_1 + b_3$$

$$b_8 = b_5(-A_2 - 1)$$

$$b_{11} = A_1 c_3 b_5 + A_2 c_4 b_5 - A_3 b_5$$

$$A_3 = \frac{A(e^{p_1}-1)}{e^{-p_1}-e^{p_1}}$$

$$A_{10} = -2b_5 A_3 - A b_5 + A_7$$

$$A_{13} = b_9 e^{p_1} - A_3 b_5 e^{-p_1} + A'$$

$$c_2 = A_1 c_3 + c_4 A_2 + A_3$$

$$b_{13} = b_5(-B_1 - 1)$$

$$b_{16} = c_7 b_5 B_1 + c_8 b_5 B_2 + b_5 B_3$$

$$B_3 = \frac{Ae^{p_1}-A}{e^{-p_1}-e^{p_1}}$$

$$A_5 = \frac{-(2+R)}{M^2}$$

$$A' = A_6 + A_7$$

$$a_3 = \frac{(1-m_1)Rb}{(1+R)(1+0.5R)}$$

$$p_1 = \frac{a_1+p}{2}$$

$$q_2 = \sqrt{\frac{a_2}{2}}$$

$$v_2 = \sqrt{\frac{\sqrt{\frac{a_1^2}{4} + \frac{p^2}{4}} - \frac{a_1}{2}}{2}}$$

$$b_3 = p_1 A_5$$

$$b_6 = b_2 + b_4$$

$$b_9 = b_5(-A_3 - A)$$

$$A_1 = \frac{e^{p_1}-e^{p_2}}{e^{-p_1}-e^{p_1}}$$

$$A_8 = -2b_5 A_1 - b_5 + b_6$$

$$A_{11} = b_7 e^{p_1} - A_1 b_5 e^{-p_1} + b_6 e^{p_2}$$

$$c_4 = \frac{A_{13}A_8 - A_{10}A_{11}}{A_{11}A_9 - A_8A_{12}}$$

$$c_1 = -c_2 - c_3 - c_4 - A$$

$$b_{14} = b_5(B_3 - A)$$

$$B_1 = \frac{e^{p_1}-\cos p_2}{e^{-p_1}-e^{p_1}}$$

$$B_4 = -2b_5 B_1 - b_5$$

$$A_6 = \frac{(1-m_1)}{M^2}$$

$$a_1 = \frac{-RbR}{(1+R)(1+0.5R)} + \frac{2Rb}{(1+0.5R)} + \frac{M^2}{(1+R)}$$

$$k = p^2 = a_1^2 - 4a_2$$

$$p_2 = \frac{a_1-p}{2}$$

$$r = \sqrt{a_1}$$

$$b_1 = p_1^3 A_4$$

$$b_4 = A_5 p_2$$

$$b_7 = b_5(-A_1 - 1)$$

$$b_{10} = c_3 b_7 + c_4 b_8 + b_9$$

$$A_2 = \frac{e^{p_1}-e^{p_2}}{e^{-p_1}-e^{p_1}}$$

$$A_9 = -2b_5 A_2 - b_5 - b_6$$

$$A_{12} = b_8 e^{p_1} - A_2 b_5 e^{-p_1} - b_6 e^{-p_2}$$

$$c_3 = \frac{A_{13}A_9 - A_{10}A_{12}}{A_{11}A_9 - A_8A_{12}}$$

$$b_{12} = b_2 - b_4$$

$$b_{15} = c_7 b_{13} + c_8 B_2 b_5 + b_{14}$$

$$B_2 = \frac{-\sin p_2}{e^{-p_1}-e^{p_1}}$$

$$B_5 = -b_2 + b_4$$

$$\begin{aligned}
B_6 &= -Ab_5 + A_7 & B_7 &= b_{13}e^{p_1} - b_5B_1e^{-p_1} + b_{12}\sin p_2 & B_8 &= b_5e^{p_1}B_2 - b_5B_2e^{-p_1} - b_{12}\cos p_2 \\
B_9 &= b_{14}e^{p_1} - b_5B_3e^{-p_1} + A_6 + A_7 & c_8 &= \frac{B_4B_9 - B_6B_7}{B_5B_7 - B_8B_4} & c_7 &= \frac{B_5B_9 - B_6B_8}{B_5B_7 - B_8B_4} \\
c_6 &= B_1c_7 + c_8B_2 + B_3 & c_5 &= -c_6 - c_7 - A & b_{17} &= b_1 - b_3 \\
b_{18} &= (-c_{11} - c_{12} - A)b_{17} & b_{19} &= b_{17}(-c_{11}B_{11} - c_{12}B_{12} - B_{13}) & B_{11} &= \frac{1-e^{p_2}}{\sin p_1} \\
B_{12} &= \frac{1-e^{-p_2}}{\sin p_1} & B_{13} &= \frac{A(\cos p_1 - 1)}{\sin p_1} & B_{14} &= -B_{11}b_{17} + b_6 \\
B_{15} &= -B_{12}b_{17} - b_6 & B_{16} &= -B_{13}b_{17} + A_7 & B_{17} &= (-\sin p_1 - B_{11}\cos p_1)b_{17} + b_6e^{p_2} \\
B_{18} &= (-\sin p_1 - A_{12}\cos p_1)b_{17} - b_6e^{-p_2} & B_{19} &= (-A\sin p_1 - A_{13}\cos p_1)b_{17} + A' & c_{12} &= \frac{B_{19}B_{15} - B_{16}B_{18}}{B_{14}B_{18} - B_{17}B_{15}} \\
c_{11} &= \frac{B_{19}B_{15} - B_{16}B_{18}}{B_{15}B_{17} - B_{18}B_{14}} & c_{10} &= B_{11}c_{11} + c_{12}B_{12} + B_{13} & c_9 &= -c_{11} - c_{12} - A \\
H_1 &= \frac{\cos p_1 - \cos p_2}{\sin p_1} & H_2 &= \frac{-\sin p_2}{\sin p_1} & H_3 &= \frac{A\cos p_1 - A}{\sin p_1} \\
b_{20} &= (-c_{15} - A)b_{17} & b_{21} &= b_{17}(-c_{15}H_1 - H_3) & H_4 &= -H_1b_{17} \\
H_5 &= H_2b_{17} - b_{12} & H_6 &= H_3b_5 + A_7 & H_7 &= (-\sin p_1 - H_1\cos p_1)b_{17} + b_{12}\sin p_2 \\
H_8 &= H_2b_{17}\cos p_1 - b_{12}\cos p_2 & c_{16} &= \frac{H_9H_4 - H_6H_7}{H_5H_7 - H_8H_4} & H_9 &= -Ab_{17}\sin p_1 - b_{17}H_3\cos p_1 + A' \\
c_{15} &= \frac{H_9H_5 - H_6H_8}{H_4H_8 - H_7H_5} & c_{14} &= H_1c_{15} - c_{16}H_2 + H_3 & c_{13} &= -c_{15} - A \\
I_1 &= \frac{e^{q_1} - e^{-q_1}}{e^{q_1}} & I_2 &= \frac{e^{-q_1}}{e^{q_1}} & I_3 &= \frac{A(e^{q_1} - 1)}{e^{q_1}} \\
b_{22} &= q_1^3 A_4 & b_{23} &= q_1^2 A_4 & b_{24} &= q_1 A_5 \\
b_{25} &= b_{22} + b_{24} & b_{26} &= 3b_{23} + A_5 & b_{27} &= b_{25} + b_{26} \\
b_{28} &= b_{25} - b_{26} & b'_{29} &= c_{19}I_1 - c_{20}I_2 + I_3 & b_{29} &= b_{25}(-c_{19} - A) + b_{26}b'_{29} \\
b_{30} &= b_{25}b'_{29} & b''_{29} &= -b_{25}c_{19} + b_{26} & b''_{30} &= -c_{20}b_{25} \\
I_4 &= -2b_{25} + I_1b_{26} & I_5 &= -I_2b_{26} + b_{26} & I_6 &= -Ab_{22} + I_3b_{26} - Ab_{24} + A_7
\end{aligned}$$

$$\begin{aligned}
I_7 &= -b_{25}(e^{q_1} + e^{-q_1}) + I_1 e^{q_1} b_{27} & I_8 &= -I_2 e^{q_1} b_{27} - e^{-q_1} b_{28} & I_9 &= -A e^{q_1} b_{25} + I_3 e^{q_1} b_{27} + A_6 + A_7 \\
c_{20} &= \frac{I_9 I_4 - I_6 I_7}{I_5 I_7 - I_8 I_4} & c_{19} &= \frac{I_9 I_5 - I_6 I_8}{I_4 I_8 - I_7 I_5} & c_{18} &= I_1 c_{19} - c_{20} I_2 + I_3 \\
c_{17} &= -c_{19} - A & J_1 &= -\tan q_1 & J_2 &= -\tan q_1 \\
J_3 &= \frac{A(\cos q_1 - 1)}{\cos q_1} & b_{31} &= 3b_{23} - A_5 & b_{32} &= b_{22} - b_{24} \\
b_{33} &= c_{23} J_1 + c_{24} J_2 + J_3 & b_{34} &= -A b_{32} & b_{35} &= b_{32} b_{33} \\
b_{36} &= -b_{31} b_{33} - c_{23} b_{32} & b_{37} &= -c_{24} b_{32} & J_4 &= -J_1 b_{31} - b_{32} \\
J_5 &= -J_2 b_{31} & J_6 &= -J_3 b_{31} + A_7 & J'_6 &= J_1 b_{31} - b_{32}, \quad J'_7 = J_2 b_{32} - b_{31} \\
J'_8 &= J_2 b_{31} - b_{32} & J'_9 &= -A b_{32} + J_3 b_{31} & J_7 &= \sin q_1 J_1 b_{32} - \cos q_1 J'_6 \\
J_8 &= \sin q_1 J'_7 - \cos q_1 J'_8 & J_9 &= \sin q_1 J'_9 - J_3 \cos q_1 b_{31} + A' & c_{24} &= \frac{J_9 J_4 - J_6 J_7}{J_5 J_7 - J_8 J_4} \\
c_{23} &= \frac{J_9 J_5 - J_6 J_8}{J_4 J_8 - J_7 J_5} & c_{22} &= J_1 c_{23} - c_{24} J_2 + J_3 & c_{21} &= -A \\
M_1 &= -\tan v_1 & M_2 &= -\tan v_1 & M_3 &= \frac{A(\cos v_1 e^{v_2} - 1)}{\cos v_1 e^{v_2}} \\
b_{38} &= v_2^2 A_4 & b_{39} &= v_2^2 v_1 A_4 & b_{40} &= v_1^2 A_4 \\
b_{41} &= v_1^3 A_4 & b_{42} &= v_1 v_2 A_4 & b_{43} &= v_1 v_2^3 A_4 \\
b_{44} &= v_2 v_1^2 A_4 & b_{45} &= v_1 A_5 & b_{46} &= v_2 A_5 \\
b'_{46} &= v_2^3 A_4 & b_{47} &= b_{38} - b_{40} & b_{48} &= 3b_{39} - b_{41} \\
b_{49} &= 3b_{44} + b_{46} & b_{50} &= A(b'_{46} + b_{49}) & b_{51} &= b_{41} - b_{45} \\
b_{52} &= 3b_{47} - b_{50} + b'_{46} + A_5 & b_{53} &= -b_{48} - 6b_{42} - b_{45} & b_{54} &= -b_{51} + 3b_{39} \\
b_{55} &= b'_{46} - b_{50} & b_{56} &= M_1 b_{52} + b_{54} & b_{57} &= M_1 b_{53} + b_{55} \\
b_{58} &= b_{54} + b_{42} & b_{59} &= b_{55} + 3b_{38} - 2b_{40} + A_5 & b_{60} &= M_2 b_{52} + b_{58} \\
b_{61} &= M_2 b_{53} + b_{59} & b_{62} &= b_{55} + (b'_{46} + A_5) & b_{63} &= A b_{50} - A b'_{46} \\
b_{64} &= M_3 b_{62} + b_{63} & b_{65} &= M_3 b_{53} + A b_{54} & b_{66} &= 3b_{47} + A_5 \\
b_{67} &= 3b_{38} - 2b_{40} + A_5 & b_{68} &= b_{48} + b_{45} & b_{69} &= M_1 c_{27} + M_2 c_{28} + M_3 \\
b_{70} &= b_{54} + b_{42} - A b_{55} & b_{71} &= b_{55} + b_{67} + A b_{68} & b_{72} &= b_{66} b_{69} + b_{70}
\end{aligned}$$

$$\begin{aligned}
b_{73} &= b_{55}b_{69} + b_{68} & b_{74} &= -b_{42}b_{69} + b_{71} & b_{75} &= -b_{68}b_{69} + b_{55} \\
M_4 &= (3b_{47} + A_5)M_1 + b_{48} + b_{45} & M_5 &= (3b_{47} + A_5)M_2 + 6b_{42} & M_6 &= (3b_{47} + A_5)M_3 - b_{50} + A_7 \\
M_7 &= (\cos v_1 b_{56} + \sin v_1 b_{57})e^{v_2} & M_8 &= e^{v_2}(\cos v_1 b_{60} + \sin v_1 b_{61}) & M_9 &= e^{v_2}(\cos v_1 b_{64} + \sin v_1 b_{65}) \\
c_{28} &= \frac{M_9 M_4 - M_6 M_7}{M_5 M_7 - M_8 M_4} & c_{27} &= \frac{M_9 M_5 - M_6 M_8}{M_4 M_8 - M_7 M_5} & c_{26} &= M_1 c_{27} + c_{28} M_2 + M_3 \\
c_{25} &= -A & L_1 &= -\tan q_2 & L_2 &= \frac{A(\cos q_2 e^{q_2} - 1)}{\cos q_2 e^{q_2}} \\
b_{77} &= q_2^3 A_4 & b_{78} &= q_2 A_5 & b_{79} &= -2b_{77} + b_{78} \\
b_{80} &= 2b_{77} + b_{78} & b_{81} &= L_1 b_{79} + L_1 A_5 & b'_{81} &= b_{81} + b_{80} \\
b'_{82} &= b_{82} + b_{79} & b'_{83} &= b'_{81} + 6b_{76} & b'_{84} &= b'_{82} + A_5 \\
b'_{85} &= b_{81} - Ab_{79} & b'_{86} &= b_{82} + Ab_{80} & b'_{87} &= c_{31} + c_{32} \\
b'_{87} &= A(A_5 - b_{79}) & b'_{88} &= -6b'_{87}L_1 - 6A & b_{82} &= -L_1 b_{80} - 6L_1 b_{76} \\
b_{83} &= c_{31}b_{80} + L_1 A_5 b'_{87} + 6c_{32}b_{76} + b'_{87} & b_{84} &= -b_{80}b_{81} + b_{79} & b_{85} &= c_{31}b_{79} - b_{76}b'_{88} + c_{32}A_5 L_1 \\
L_4 &= 2b_{77} + A_5 L_1 + b_{79} & L_5 &= 6b_{76} + A_5 L_1 & L_6 &= 2Ab_{77} - Ab_{79} + A_5 L_2 + A_7 \\
L_7 &= (\cos q_2 b'_{81} + \sin q_2 b'_{82})e^{q_2} & L_8 &= (\cos q_2 b'_{83} + \sin q_2 b'_{84})e^{q_2} & L_9 &= (\cos q_2 b'_{85} + \sin q_2 b'_{86})e^{q_2} + A' \\
c_{32} &= \frac{L_9 L_4 - L_6 L_7}{L_5 L_7 - L_8 L_4} & c_{31} &= \frac{L_9 L_5 - L_6 L_8}{L_4 L_8 - L_7 L_5} & c_{30} &= L_1 c_{31} + c_{32} L_1 + L_2 \\
c_{29} &= -A & G_1 &= \frac{\cos r - e^r}{e^r - e^{-r}} & G_2 &= \frac{\sin r}{e^r - e^{-r}} \\
G_3 &= \frac{(a_3/2a_1)}{e^r - e^{-r}} & b_{86} &= r^3 A_4 & b_{87} &= A_5 r \\
b_{88} &= b_{86} b_{87} & b_{89} &= b_{86} - b_{87} & b_{90} &= -G_1 c_{35} - G_2 c_{36} + G_3 \\
b_{91} &= b_{88} b_{90} & b_{92} &= c_{35} b_{89} & b_{93} &= c_{36} b_{89} \\
b_{94} &= A_6 - \frac{a_3}{a_1} & G_4 &= (-2G_1 - 1)b_{88} & G_5 &= -2G_2 b_{88} - b_{89} \\
G_6 &= 2G_3 b_{88} + A_7 & G_7 &= b_{88}(G_1(-e^r - e^{-r}) - e^r) + \sin r b_{89} & G_8 &= b_{88} G_2(-e^r - e^{-r}) + \cos r b_{89} \\
G_9 &= b_{88} G_3(-e^r - e^{-r}) - \frac{a_3}{a_1} + A' & c_{36} &= \frac{G_9 G_4 - G_6 G_7}{G_5 G_7 - G_8 G_4} & c_{35} &= \frac{G_9 G_5 - G_6 G_8}{G_4 G_8 - G_7 G_5} \\
c_{34} &= G_1 c_{35} + c_{36} G_2 - G_3 & c_{33} &= -c_{34} - c_{35} & b_{95} &= \frac{a_3}{6}
\end{aligned}$$

$$b_{96} = 3c_{40}$$

$$b_{97} = 2c_{39} + A_6 + A_4 a_3$$

$$b_{98} = c_{39} + c_{40} + \frac{a_3}{24}$$

$$b_{99} = 6c_{40}A_4 - b_{98}A_5 + A_7$$

$$D_1 = -A_5 ,$$

$$D_2 = -6A_4$$

$$D_3 = \frac{-25a_3}{24} + A_7$$

$$D_4 = D_1 + 2$$

$$D_5 = D_2 + D_1 + 3$$

$$D_6 = A_4 c_{39} - \frac{A_5 a_3}{24} + b_{95} + A_6 + A_7$$

$$c_{40} = \frac{D_6 D_1 - D_3 D_4}{D_2 D_4 - D_5 D_1}$$

$$c_{39} = \frac{D_6 D_2 - D_3 D_5}{D_1 D_5 - D_4 D_2}$$

$$c_{38} = -c_{39} - c_{40} - \frac{a_3}{24}$$

$$c_{37} = 0$$

Chapter 3, Section-I

$$a = 1 + \frac{1}{\gamma}$$

$$b = M^2 + \frac{1}{k}$$

$$d = apr - 1$$

$$e = aSc - 1$$

$$f = \frac{b}{d}$$

$$g = \frac{b}{e}$$

$$a_1 = \frac{Gr}{d f}$$

$$a_3 = -\frac{Gr}{d f}$$

$$a_2 = \frac{Gr}{d(1-f)} - \frac{a_1}{1-f} - a_3$$

$$a_5 = \frac{Gm}{ge^2}$$

$$a_6 = \frac{Gm}{eg^2}$$

$$a_4 = \frac{Gm}{e(1-g)} - a_5 - \frac{a_6}{1-g}$$

Chapter 4, Section-I

$$a = 1 + \frac{1}{\gamma}$$

$$b = M^2 + \frac{1}{k}$$

$$a_1 = aNr - b$$

$$a_2 = aPr - 1$$

$$a_3 = \frac{a_1}{a_2}$$

$$a_4 = a Sc Kr - b$$

$$a_5 = aSc - 1$$

$$a_6 = \frac{a_4}{a_5}$$

$$a_7 = \frac{Gr}{a_2 a_3^2}$$

$$a_9 = \frac{Gr}{a_2 a_3}$$

$$a_{11} = \frac{Gm}{a_5 a_6^2}$$

$$a_8 = \frac{Gr}{a_2(1+a_3)} - \frac{a_4}{1+a_3} - a_6$$

$$a_{12} = \frac{Gm}{a_5 a_6}$$

$$a_{10} = \frac{Gm}{a_5(1+a_6)} - a_8 - \frac{a_9}{1+a_6}$$

Chapter 4, Section-II

$$a = 1 + \frac{1}{\gamma}$$

$$b = M^2 + \frac{1}{k}$$

$$d = \frac{(1+Nr)}{Pr}$$

$$a_1 = \frac{a}{d} - 1$$

$$a_2 = \frac{b}{a_1}$$

$$a_3 = \frac{Gr}{a_1}$$

$$a_4 = a Sc - 1$$

$$a_5 = a Sc Kr - b$$

$$a_6 = \frac{a_5}{a_4}$$

$$a_7 = \frac{Gm}{a_4}$$

$$a_{11} = \frac{a_7}{a_6}$$

$$a_{14} = a_{10} + a_{13}$$

$$a_8 = -\frac{a_3}{a_2}$$

$$a_{12} = \frac{a_7}{a_6^2}$$

$$a_{15} = a_8 + a_{11}$$

$$a_9 = \frac{a_3}{a_2^2}$$

$$a_{10} = \frac{a_3}{(1-a_2)} - a_8 - \frac{a_9}{(1-a_2)}$$

$$a_{13} = \frac{a_7}{(1+a_6)} - a_{11} - \frac{a_{12}}{(1+a_6)}$$

Chapter 5

$$a = 1 + \frac{1}{\gamma}$$

$$a_2 = a \, Pr \, c + b$$

$$a_5 = a \, Sc - 1$$

$$a_8 = \frac{Gm}{a_5}$$

$$a_{12} = \frac{a_8}{a_{12}}$$

$$a_{16} = a_9 + a_{12}$$

$$b = M^2 + \frac{1}{k}$$

$$a_3 = \frac{a_2}{a_1}$$

$$a_6 = a \, ScKr - b$$

$$a_9 = -\frac{a_4}{a_3}$$

$$a_{13} = \frac{a_8}{a_7^2}$$

$$a_{15} = a_{11} + a_{14}$$

$$a_1 = a \, Pr - 1$$

$$a_4 = \frac{Gr}{a_1}$$

$$a_7 = \frac{a_6}{a_5}$$

$$a_{10} = \frac{a_4}{a_3^2}$$

$$a_{11} = \frac{a_4}{(1-a_3)} - a_9 - \frac{a_{10}}{(1-a_3)}$$

$$a_{14} = \frac{a_8}{(1+a_7)} - a_{12} - \frac{a_{13}}{(1+a_7)}$$

Chapter 6, Section-I

$$a = 1 + \frac{1}{\gamma}$$

$$d = Gm$$

$$a_8 = \frac{1}{Sc}$$

$$a_{11} = \frac{a_8}{a_6}$$

$$b_{14} = a_{11} - 1$$

$$a_{16} = \frac{a_{14}}{b_{14}}$$

$$a_{20} = \frac{a}{a_6}$$

$$b_{21} = a_{20} - 1$$

$$a_{24} = \frac{c}{b_{21}}$$

$$b = M^2 + \frac{1}{k}$$

$$a_6 = \frac{1}{Pr}$$

$$a_9 = Sr$$

$$a_{12} = \frac{a_7}{a_6}$$

$$a_{14} = \frac{a_9}{a_6}$$

$$a_{17} = \frac{-a_{16} \, a_7}{a_{15}}$$

$$a_{21} = \frac{a \cdot a_7}{a_6}$$

$$a_{22} = b + a_{21}$$

$$b_{24} = \frac{a}{a_8} - 1$$

$$c = Gr$$

$$a_7 = \frac{H-R}{Pr}$$

$$a_{10} = Kr$$

$$a_{13} = a_{10} - a_{12}$$

$$a_{15} = \frac{a_{13}}{b_{14}}$$

$$a_{18} = \frac{-a_{16} \, (a_{15} + a_7)}{a_{15}^2}$$

$$a_{19} = \frac{a_{16} \, (1-a_7)}{1+a_{15}} - a_{17} - \frac{a_{18}}{1+a_{15}}$$

$$a_{23} = \frac{a_{22}}{b_{21}}$$

$$a_{25} = \frac{a \, a_{10}}{a_8} + b$$

$$a_{26} = \frac{a_{25}}{b_{24}}$$

$$a_{27} = \frac{d}{b_{24}}$$

$$a_{28} = \frac{d a_{16}}{b_{24}}$$

$$a_{29} = \frac{d a_{16}}{b_{21}}$$

$$a_{30} = \frac{-a_{24}}{a_{23}}$$

$$a_{31} = \frac{a_{24}}{a_{23}^2}$$

$$a_{33} = \frac{-a_{27}}{a_{26}}$$

$$a_{34} = \frac{a_{27}}{a_{26}^2}$$

$$a_{32} = \frac{a_{24}}{1-a_{23}} - a_{30} - \frac{a_{31}}{1-a_{23}}$$

$$a_{36} = \frac{a_{28} a_7}{a_{15} a_{26}}$$

$$a_{37} = \frac{a_{28} (a_7 + a_{15})}{a_{15}^2 (a_{26} + a_{15})}$$

$$a_{35} = \frac{a_{27}}{1-a_{26}} - a_{33} - \frac{a_{34}}{1-a_{26}}$$

$$a_{38} = \frac{a_{28} (a_{26} - a_7)}{a_{26}^2 (a_{26} + a_{15})}$$

$$a_{40} = \frac{a_{29} a_7}{a_{15} a_{23}}$$

$$a_{39} = \frac{a_{28} (1-a_7)}{(1-a_{26})(1+a_{15})} - a_{36} - \frac{a_{37}}{1+a_{15}} - \frac{a_{38}}{1-a_{26}}$$

$$a_{41} = \frac{a_{29} (a_7 + a_{15})}{a_{15}^2 (a_{23} + a_{15})}$$

$$a_{42} = \frac{a_{29} (a_{23} - a_7)}{a_{23}^2 (a_{23} + a_{15})}$$

$$a_{43} = \frac{a_{29} (1-a_7)}{(1-a_{23})(1+a_{15})} - a_{40} - \frac{a_{41}}{1+a_{15}} - \frac{a_{42}}{1-a_{23}}$$

$$a_{46} = a_{31} - a_{42}$$

$$a_{47} = a_{35} + a_{38}$$

$$a_{44} = a_{32} + a_{35} + a_{39} - a_{43}$$

$$a_{48} = a_{37} - a_{41}$$

$$a_{49} = a_{43} - a_{32}$$

$$a_{45} = a_{30} + a_{33} + a_{36} - a_{40}$$

$$a_{50} = a_{40} - a_{30}$$

$$a_{51} = a_{42} - a_{31}$$

$$a_{52} = -a_{35} - a_{39}$$

$$a_{53} = -a_{33} - a_{36}$$

$$a_{54} = -a_{34} - a_{38}$$

$$a_{55} = \frac{-a_{28} (a_{15} + a_7)}{a_{15} (a_{26} + a_{15})}$$

$$a_{56} = \frac{a_{28} (a_{26} - a_7)}{a_{26} (a_{26} + a_{15})}$$

$$a_{57} = \frac{-a_{29} (a_{15} + a_7)}{a_{15} (a_{23} + a_{15})}$$

$$a_{58} = \frac{a_{29} (a_{23} - a_7)}{a_{23} (a_{23} + a_{15})}$$

$$a_{59} = a_{30} + a_{36} - a_{40}$$

$$a_{60} = -a_{30} - a_{58}$$

$$a_{61} = a_{55} - a_{57}$$

$$a_{62} = a_{30} + a_{58}$$

$$a_{63} = \frac{a_{16} (a_{15} + a_7)}{a_{15}}$$

$$a_{64} = a_{33} - a_{56}$$

$$F_1(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{s+iw}$$

$$F_2(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{s-iw}$$

$$F_3(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{s}$$

$$F_4(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{s^2}$$

$$F_5(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{s-a_{23}}$$

$$F_6(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{(s-a_{26})}$$

$$F_7(y, s) = \frac{e^{-y\sqrt{\frac{s+b}{a}}}}{(s+a_{15})}$$

$$F_8(y, s) = \frac{e^{-y\sqrt{\frac{s-a_7}{a_6}}}}{s}$$

$$F_9(y, s) = \frac{e^{-y\sqrt{\frac{s-a_7}{a_6}}}}{s^2}$$

$$F_{10}(y, s) = \frac{e^{-y\sqrt{\frac{s-a_7}{a_6}}}}{(s-a_{23})}$$

$$F_{11}(y, s) = \frac{e^{-y\sqrt{\frac{s-a_7}{a_6}}}}{(s+a_{15})}$$

$$F_{12}(y, s) = \frac{1}{s} e^{-y\sqrt{\frac{s-a_{10}}{a_8}}}$$

$$F_{13}(y, s) = \frac{1}{s^2} e^{-y \sqrt{\frac{s-a_{10}}{a_8}}} \quad F_{14}(y, s) = \frac{e^{-y \sqrt{\frac{s-a_{10}}{a_8}}}}{(s-a_{26})} \quad F_{15}(y, s) = \frac{e^{-y \sqrt{\frac{s-a_{10}}{a_8}}}}{(s+a_{15})}$$

$$f_i(y, t) = L^{-1} F_i(y, s), i = 1 \text{ to } 15 \quad h_i(y, t) = L^{-1} H_i(y, s), i = 1 \text{ to } 3 \quad g_i(y, t) = L^{-1} G_i(y, s), i = 1 \text{ to } 15$$

$$h_1 = g_2 + g_3 + g_4 \quad h_2 = f_{13} + g_{10} + g_{11} \quad h_3 = g_1 + g_7 + g_{14} + g_{15}$$

$$g_1 = \frac{i}{2} f_1 - \frac{i}{2} f_2 \quad g_6 = a_{35} f_3 + a_{33} f_4 + a_{34} f_6 \quad g_2 = a_{44} f_3 + a_{45} f_4 + a_{46} f_5 + a_{47} f_6 + a_{48} f_7$$

$$g_{11} = a_{19} f_8 + a_{17} f_9 + a_8 f_{11} \quad g_5 = a_{59} f_3 + a_{60} f_5 + a_{61} f_7 + a_{56} f_6 \quad g_3 = a_{49} f_8 + a_{50} f_9 + a_{51} f_{10} + a_{41} f_{11}$$

$$g_{12} = a_{17} f_{12} + a_{63} f_{15} \quad g_7 = a_{50} f_8 + a_{62} f_{10} + a_{57} f_{11} \quad g_4 = a_{52} f_{12} + a_{53} f_{13} + a_{54} f_{14} - a_{37} f_{15}$$

$$g_{13} = a_{17} f_8 + a_{63} f_{11} \quad g_8 = a_{35} f_{12} + a_{33} f_{13} + a_{34} f_{14} \quad g_9 = a_{36} f_{12} + a_{55} f_{15} + a_{56} f_{14}$$

$$g_{15} = a_{53} f_{12} - a_{55} f_{15} - a_{64} f_{14} \quad g_{10} = a_{19} f_{12} + a_{17} f_{13} + a_8 f_{15} \quad g_{14} = a_{45} f_3 + a_{60} f_5 + a_{64} f_6 + a_{61} f_7$$

$$J_1 = \left. \frac{df_1}{dy} \right|_{y=0} \dots J_{15} = \left. \frac{df_{13}}{dy} \right|_{y=0} \quad J_{16} = \left. \frac{dg_1}{dy} \right|_{y=0} \dots J_{30} = \left. \frac{dg_{15}}{dy} \right|_{y=0} \quad J_{31} = \left. \frac{dh_1}{dy} \right|_{y=0} \dots J_{33} = \left. \frac{dh_3}{dy} \right|_{y=0}$$

$$L^{-1} \left(\frac{e^{-y\sqrt{s+b}}}{s} \right) = \frac{1}{2} \left[e^{-y\sqrt{b}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} - \sqrt{bt} \right) + e^{y\sqrt{b}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} + \sqrt{bt} \right) \right]$$

$$L^{-1} \left(\frac{e^{-y\sqrt{s+b}}}{s^2} \right) = \frac{1}{2} \left[\left(t - \frac{y}{2\sqrt{b}} \right) e^{-y\sqrt{b}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} - \sqrt{bt} \right) + \left(t + \frac{y}{2\sqrt{b}} \right) e^{y\sqrt{b}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} + \sqrt{bt} \right) \right]$$

$$L^{-1} \left(\frac{e^{-y\sqrt{s+b}}}{(s+a)} \right) = \frac{e^{-at}}{2} \left[e^{-y\sqrt{\frac{1}{a}(b-a)}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} - \sqrt{(b-a)t} \right) + e^{y\sqrt{\frac{1}{a}(b-a)}} \operatorname{erfc} \left(\frac{y}{2\sqrt{t}} + \sqrt{(b-a)t} \right) \right]$$

Chapter 6, Section-II

$$c = 1 + \frac{\alpha}{k_1} \quad b = M^2 + \frac{1}{k_1} \quad a_1 = \frac{-H}{1+R}, \quad L = \frac{\operatorname{Pr}}{1+R}$$

$$a_2 = a_1 - Kr.Sc \quad a_3 = L - Sc \quad a_4 = \frac{a_2}{a_3}$$

$$a_5 = \frac{Sr.Sc}{a_3} \quad a_6 = \frac{a_1 a_5}{a_4} \quad a_7 = \frac{a_5 (a_1 - a_4 L)}{a_4^2}$$

$$\begin{aligned}
a_{10} &= \frac{Gm}{b_9(b_9-b_{10})} & a_9 &= \frac{Gm}{b_9 b_{10}} & a_8 &= \frac{a_5(a_1+L)}{1+a_4} - a_6 - \frac{a_7}{1+a_4} \\
a_{11} &= \frac{Gm}{b_{10}(b_{10}-b_9)} & a_{12} &= \frac{Gm a_1 a_5}{a_4 b_9 b_{10}} & a_{13} &= \frac{Gm a_5(a_1-a_4 L)}{(-a_4)(b_9+a_4)(a_4+b_{10})} \\
a_{14} &= \frac{Gm a_5(a_1+b_9 L)}{(b_9)(b_9+a_4)(b_9-b_{10})} & a_{16} &= \frac{Gr}{b_4 b_5} & a_{15} &= \frac{Gm a_5(a_1+b_{10} L)}{(b_{10})(b_{10}+a_4)(b_{10}-b_9)} \\
a_{17} &= \frac{Gr}{(b_4)(b_4-b_5)} & a_{18} &= \frac{Gr}{(b_5)(b_5-b_4)} & a_{21} &= \frac{Gm a_5(a_1+b_4 L)}{(b_4)(b_4+a_4)(b_4-b_5)} \\
a_{20} &= \frac{Gm a_5(a_1-a_4 L)}{(-a_4)(b_4+a_4)(a_4+b_5)} & a_{19} &= \frac{Gm a_1 a_5}{a_4 b_4 b_5} & a_{22} &= \frac{Gm a_5(a_1+b_5 L)}{(b_5)(b_5+a_4)(b_5-b_4)} \\
a_{23} &= a_9 + a_{12} & a_{24} &= a_{10} + a_{14} & a_{25} &= a_{11} + a_{15} \\
a_{26} &= a_{16} - a_{19} & a_{27} &= a_{17} - a_{21} & a_{28} &= a_{18} - a_{22} \\
a_{29} &= \frac{Gr}{(b_4-b_5)} & a_{30} &= \frac{Gm a_5(a_1-a_4 L)}{(b_9+a_4)(a_4+b_{10})} & a_{31} &= \frac{Gm a_5(a_1+b_9 L)}{(b_9+a_4)(b_9-b_{10})} \\
a_{32} &= \frac{Gm a_5(a_1+b_{10} L)}{(b_{10}+a_4)(b_{10}-b_9)} & a_{33} &= \frac{Gm a_5(a_1-a_4 L)}{(b_4+a_4)(a_4+b_5)} & a_{34} &= \frac{Gm a_5(a_1+b_4 L)}{(b_4+a_4)(b_4-b_5)} \\
a_{35} &= \frac{Gm a_5(a_1+b_5 L)}{(b_5+a_4)(b_5-b_4)} & a_{36} &= a_{29} - a_{34} & a_{37} &= -a_{29} - a_{35} \\
a_{38} &= \frac{a_5(a_1-a_4 L)}{(-a_4)} & b_1 &= \alpha L & b_2 &= L + \alpha a_1 - c \\
b_3 &= a_1 - b & b_4 &= \frac{-b_2 + \sqrt{b_2^2 - 4b_1 b_3}}{2b_1} & b_5 &= \frac{-b_2 - \sqrt{b_2^2 - 4b_1 b_3}}{2b_1} \\
b_6 &= \alpha Sc & b_7 &= Sc + \alpha kr Sc - c & b_8 &= Kr Sc - b \\
b_9 &= \frac{-b_7 + \sqrt{b_7^2 - 4b_6 b_8}}{2b_6} & b_{10} &= \frac{-b_7 - \sqrt{b_7^2 - 4b_6 b_8}}{2b_6}
\end{aligned}$$

Chapter 7, Section-I

$$\begin{aligned}
a &= 1 + \frac{1}{\gamma} & a_2 &= \frac{1+Nr}{Pr} & a_1 &= \frac{M^2(1-im)}{1+m^2} + \frac{1}{k} - 2ik_1^2 \\
a_3 &= \frac{1}{Sc} & a_4 &= \frac{a}{a_2} - 1 & a_8 &= \frac{a}{a_3} - 1 \\
a_6 &= \frac{a_5}{a_4} & a_7 &= \frac{Gr}{a_4} & a_9 &= \frac{aKr}{a_3} - a_1 \\
a_{10} &= \frac{a_9}{a_8} & a_{11} &= \frac{Gm}{a_8} & a_{14} &= \frac{a_7}{(1-a_6)} - a_{12} - \frac{a_{13}}{(1-a_6)}
\end{aligned}$$

$$a_{12} = -\frac{a_7}{a_6}$$

$$a_{13} = \frac{a_7}{a_6^2}$$

$$a_{17} = \frac{a_{11}}{(1+a_{10})} - a_{15} - \frac{a_{16}}{(1+a_{10})}$$

$$a_{15} = \frac{a_{11}}{a_{10}}$$

$$a_{16} = \frac{a_{11}}{a_{10}^2}$$

Chapter 7, Section-II

$$a = 1 + \frac{1}{\gamma}$$

$$c = \frac{(1+R)}{Pr}$$

$$b = \frac{M^2(1-im)}{1+m^2} + \frac{1}{k_1} - 2ik^2$$

$$d = \frac{H}{pr}$$

$$a_1 = \frac{Sr.Sc}{c}$$

$$a_2 = \frac{1}{c} - Sc$$

$$a_3 = \frac{d}{c} + Kr.Sc$$

$$a_4 = \frac{a_3}{a_2}$$

$$a_5 = -\frac{a_1}{a_2}$$

$$a_6 = \frac{a}{c} - 1$$

$$a_7 = \frac{a}{c} d + b$$

$$a_8 = \frac{a_7}{a_6}$$

$$a_9 = \frac{Gr}{a_6}$$

$$a_{10} = aSc - 1$$

$$a_{11} = Sc \ Kr \ a - b$$