

pts	Age-points					$\sum X_s$	$(\sum X_s)^2$	P_1	P_1^2	P_2	P_2^2	P_3	P_3^2	P_4	P_4^2
	2-0	2-3	2-6	2-9	3-0										
1	12.5	12.5	13.5	14.0	14.5	57	1489.0	5.5	30.25	0.5	00.25	-1.0	1.00	2.0	04.00
2	11.0	11.5	12.5	13.0	13.5	61.5	3782.25	6.5	42.25	-0.5	00.25	-0.5	0.25	1.5	02.25
3	9.0	9.5	10.5	9.5	10.5	49.0	2401.0	3.0	09.00	-1.0	1.00	1.5	2.25	6.5	42.25
4	9.0	9.5	10.0	10.5	11.0	50.0	2500.0	7.0	49.00	0.00	0.00	0.00	0.00	0.00	0.00
5	10.5	11.0	11.5	12.0	13.0	58	3364.0	6.0	36.00	1.0	1.00	0.5	0.25	0.5	0.25
6	11.5	11.5	12.0	12.5	13.0	60.5	3660.25	4.0	16.00	1.0	1.00	-0.5	0.25	0.5	0.25
7	9.5	9.5	11.0	10.5	11.0	51.5	2652.25	4.0	16.00	-1.0	1.00	-0.5	0.25	6.5	42.25
8	6.5	8.5	8.5	8.5	9.5	41.5	1722.25	6.0	36.00	-2.0	4.00	3.0	9.00	-1.0	1.00
9	9.0	10.0	10.0	11.0	10.5	50.5	2550.25	4.0	16.00	-2.0	4.00	-0.5	0.25	-4.5	20.25
10	10.5	10.5	11.5	11.5	12.0	56	3136.0	4.0	16.00	0.0	0.00	-0.5	0.25	3.5	12.25
11	9.5	10.0	10.5	10.5	11.0	51.5	2652.25	3.5	12.25	-0.5	0.25	0.5	0.25	1.5	2.25
12	10.5	11.5	11.5	12.0	12.0	57.5	3306.25	3.5	12.25	-1.5	2.25	0.5	0.25	-2.5	6.25
13	12.5	13.5	13.5	14.0	14.5	68	4624.0	4.5	20.25	-0.5	0.25	1.0	1.00	-2.0	4.00
14	7.5	8.5	9.0	9.0	10.0	44	1936.0	5.5	30.25	-0.5	0.25	1.5	2.25	1.5	2.25
15	9.5	10.5	11.0	11.0	11.5	54.0	2916.0	4.5	20.25	-1.5	2.25	1.0	1.00	1.0	1.00
16	9.0	9.5	9.5	10.0	10.5	48.5	2352.25	3.5	12.25	0.5	0.25	0.5	0.25	-1.5	2.25
17	10.5	10.8	11.1	11.9	12.5	56.8	3226.24	5.1	26.01	1.1	1.21	-0.2	0.04	-1.2	1.44
18	12.5	13.0	13.5	14.0	14.0	67.0	4489.0	4.0	16.00	-1.0	1.00	-0.5	0.25	-0.5	0.25
19	11.0	11.5	11.5	12.0	12.5	58.5	3422.25	3.5	12.25	0.5	0.25	0.5	0.25	-1.5	2.25
20	10.5	11.5	12.0	12.5	13.5	60.0	3600.0	7.0	49.00	0.0	0.0	1.0	1.00	0.0	0.0
21	9.5	12.0	11.0	12.0	13.0	57.5	3306.25	7.0	49.00	1.0	1.00	3.5	12.25	-7.5	56.25
22	9.5	10.0	10.5	11.5	11.5	53.0	2809.0	5.5	30.25	-0.5	0.25	-1.0	1.00	-2.0	4.00
23	11.5	12.0	12.0	12.0	12.0	59.5	3540.25	1.0	1.00	1.0	1.00	0.5	0.25	-0.5	0.25
24	11.5	11.5	11.5	13.0	12.5	60.0	3600	3.5	12.25	0.5	0.25	-2.0	4.00	-5.0	25.00
25	9.5	10.0	10.5	11.5	11.5	53	2809.0	5.5	30.25	-0.5	0.25	-1.0	1.00	-2.0	4.00
26	11.0	11.5	11.5	12.0	12.0	58	3364.0	2.5	6.25	-0.5	0.25	0.0	0.0	-2.0	4.00
27	10.5	10.0	11.0	10.5	12.0	54	2916.0	3.5	12.25	2.5	6.25	0.5	0.25	6.5	42.25
28	11.0	11.5	11.0	11.5	12.0	57	3249.0	2.0	4.0	1.0	1.00	1.0	1.00	-3.0	9.0
29	9.5	9.5	11.0	11.5	12.0	53.5	2862.25	7.0	49.0	0.0	0.0	-1.5	2.25	3.5	12.25

Total 335.5 310.0 324.1 334.9 349.0 1615.8 91237.24 132.1 671.51 -2.9 30.71 7.3 42.29 -1.7 303.69

$\sum X_{A1}$ $\sum X_{A2}$ $\sum X_{A3}$ $\sum X_{A4}$ $\sum X_{A5}$ $\sum X$ $\sum (\sum X_s)^2$ $\sum P_1$ $\sum (\sum P_1)^2$ $\sum P_2$ $\sum (\sum P_2)^2$ $\sum P_3$ $\sum (\sum P_3)^2$ $\sum P_4$ $\sum (\sum P_4)^2$

$(\sum X_{A1})^2 = 87320.25$; $(\sum X_{A2})^2 = 97531.29$; $(\sum X_{A3})^2 = 105040.81$; $(\sum X_{A4})^2 = 112158.01$;

$(\sum X_{A5})^2 = 121801.00$.

$N = 145$ $n_s = 29$ $N_A = 5$ $\sum X = 1615.8$ $(\sum X)^2 = 2610809.64$ $\sum X^2 = 18420.00$
 $\sum (\sum X_s)^2 = 91237.24$ $\sum (\sum X_s)^2 = 523851.36$

Values of Orthogonal Polynomials (ϕ) for Trend Analysis

Poly. Coef.	Age stages					$\sum \phi^2$
	2-0	2-3	2-6	2-9	3-0	
1	-2	-1	0	1	2	10
2	2	-1	-2	-1	2	14
3	-1	2	0	-2	1	10
4	1	-4	6	-4	1	70

Appendix - 6 Contd.Procedure for Analysis

(1) First treat the above data as if in a 5 x 29 factorial design : age-points x Subjects, each score of one observation forming a cell i.e. with a total $N = 5 \times 29 = 145$ and subject these data to the statistical technique of analysis of variance. Thus, the following values would be computed as per procedure of analysis of variance.

$$(i) \quad \Sigma X = 1615.80$$

$$(ii) \quad C = (\Sigma X)^2 / N = 1615.8^2 / 145 = 18005.51$$

$$(iii) \quad \Sigma X^2 = 18420.00$$

$$(iv) \quad SS \text{ Total} = \Sigma X^2 - C = 18420.00 - 18005.51 = 414.49$$

$$\begin{aligned} (v) \quad SS \text{ Age} &= (\Sigma X_{A1})^2 + \dots + (\Sigma X_{A5})^2 - C \\ &= (295.5)^2 + \dots + (349.0)^2 - 18005.51 \\ &= 18063.84 - 18005.51 \\ &= 58.33 \end{aligned}$$

$$\begin{aligned} (vi) \quad SS \text{ Sub.} &= (\Sigma X_{S1})^2 + \dots + (\Sigma X_{S29})^2 - C \\ &= (67.0)^2 + \dots + (53.5)^2 - 18005.51 \\ &= 18247.45 - 18005.51 \\ &= 241.94 \end{aligned}$$

$$(vii) \quad SS_{A \times S} = SS_T - SS_A - SS_S$$

$$\begin{aligned} (\text{error term in this case}) &= 414.49 - 58.33 - 241.94 \end{aligned}$$

(2) Next, compute the following values of polynomials :

(i) P_1, P_2, P_3, P_4 where $P_1 = (\sum X_i \phi_i)$

i.e. multiply each of five scores of a subject by respective value of ϕ at that stage and summate these five products e.g. separately for each subject.

e.g.

P_1 for subject no. 1 =

$$(-2)(12.5) + (-1)(12.5) + (0)(13.5) + (+1)(14.0) + (+2)(14.5) \\ = -25.0 - 12.5 + 0 + 14.0 + 29.0 = 5.5$$

and so on for other subjects.

Similarly, P_2 for subject no. 1 =

$$(+2)(12.5) + (-1)(12.5) + (-2)(13.5) + (-1)(14.0) + (+2)(14.5) \\ = 25.0 - 12.5 - 27.0 - 14.0 + 29.0 = 0.5$$

and so on for other subjects.

P_3 for subject no. 1 =

$$(-1)(12.5) + (+2)(12.5) + (0)(13.5) + (-2)(14.0) + (+1)(14.5) \\ = -12.5 + 25.0 + 0 - 28.0 + 14.5 = 1.0$$

and so on for other subjects.

P_4 for subject no. 1 =

$$(+1)(12.5) + (-4)(12.5) + (+6)(13.5) + (-4)(14.0) + (+1)(14.5) \\ = 12.5 - 50.0 + 81.0 - 56.0 + 14.5 = 2.0$$

and similarly for other subjects.

All these values are entered into column under $P_1, P_2, P_3,$

and P_4 in data sheet for each subject. These values for each subject are squared and entered under respective columns P_1^2 , P_2^2 , P_3^2 , and P_4^2 in data sheet. Values in each of columns are summated and entered under appropriate row at end. Thus, is prepared the whole data sheet.

(3) Next the following values for trend analysis are computed thus :

$$(i) U_y = \sum X^2 = 18420.00 \dots (\text{as in } SS_{Tot})$$

$$(ii) U_I = (\sum X_{S1})^2 + \dots + (\sum X_{S29})^2 / n_s$$

$$= (67.0)^2 + \dots + (53.5)^2 / 5$$

$$= 18247.45 \dots (\text{As in } SS_{sub}).$$

$$(iii) U_{P_1} = (P_{1.1})^2 + (P_{1.2})^2 + \dots + (P_{1.29})^2 / \phi_1^2$$

$$= (5.5)^2 + \dots + (7.0)^2 / 10 = 671.51 / 10 = 67.151$$

$$(iv) U_{P_2} = (P_{2.1})^2 + (P_{2.2})^2 + \dots + (P_{2.29})^2 / \phi_2^2$$

$$= (0.5)^2 + \dots + (0.0)^2 / 14 = 30.71 / 14 = 2.19$$

$$(v) U_{P_3} = (P_{3.1})^2 + (P_{3.2})^2 + \dots + (P_{3.29})^2 / \phi_3^2$$

$$= 42.19 / 10 = 4.219$$

$$(vi) U_{P_4} = (P_{4.1})^2 + (P_{4.2})^2 + \dots + (P_{4.29})^2 / \phi_4^2$$

$$= 303.69 / 70 = 4.338$$

$$(vii) W_y = (\sum X_{A_1})^2 + \dots + (\sum X_{A_s})^2 / n_a$$

$$= (295.5)^2 + \dots + (349.0)^2 / 29$$

$$= 523851.36 / 29 = 18063.84 \dots (\text{as in } SS_{Age})$$

$$\begin{aligned} \text{(viii) } W_I &= (\sum X)^2/N = (1615.8)^2/145 = 2610809.64/145 \\ &= 18005.51 \dots\dots\dots(\text{Same as correction term}). \end{aligned}$$

$$\begin{aligned} \text{(ix) } W_{P_1} &= (\sum P_1)^2/n_s \phi_1^2 = (132.1)^2/29 \times 10 \\ &= 17450.41/290 = 60.17. \end{aligned}$$

$$\begin{aligned} \text{(x) } W_{P_2} &= (\sum P_2)^2/n_s \phi_2^2 = (-2.9)^2/29 \times 14 \\ &= 8.41/406 = 0.21. \end{aligned}$$

$$\begin{aligned} \text{(xi) } W_{P_3} &= (\sum P_3)^2/n_s \phi_3^2 = (7.3)^2/29 \times 10 \\ &= 53.29/290 = 0.13. \end{aligned}$$

$$\begin{aligned} \text{(xii) } W_{P_4} &= (\sum P_4)^2/n_s \phi_4^2 = (-1.7)^2 \times 29 \times 70 \\ &= 1.89/2030 = 0.001. \end{aligned}$$

- (4) Finally, on the basis of the above values, prepare a table showing a summary of results of analysis of variance (including significance of trend) (see Table 5.7).